

Propagation of large concentration changes in reversible protein binding networks

Sergei Maslov * †, I. Ispolatov ‡ §

*Department of Condensed Matter Physics and Materials Science, Brookhaven National Laboratory, Upton, New York 11973, USA, and †Ariadne Genomics, Inc., 9430 Key West Ave, Suite 113, Rockville, Maryland 20850, USA

Submitted to Proceedings of the National Academy of Sciences of the United States of America

We study how the dynamic equilibrium of the reversible protein-protein binding network in yeast *S. cerevisiae* responds to large changes in abundances of individual proteins. The magnitude of shifts between free and bound concentrations of their immediate and more distant neighbors in the network is influenced by such factors as the network topology, the distribution of protein concentrations among its nodes, and the average binding strength. Our primary conclusion is that on average the effects of a perturbation are strongly localized and exponentially decay with the network distance away from the perturbed node. This explains why, despite globally connected topology, individual functional modules in such networks are able to operate fairly independently. We also found that under specific favorable conditions, realized in a significant number of paths in the yeast network, concentration perturbations can selectively propagate over considerable network distances (up to four steps). Such "action-at-a-distance" requires high concentrations of heterodimers along the path as well as low free (unbound) concentration of intermediate proteins.

law of mass action | genetic interactions | dissociation constant | small-world networks | binding equilibrium

Introduction

Recent high-throughput experiments performed in a wide variety of organisms revealed networks of protein-protein physical interactions (PPI) that are interconnected on a genome-wide scale. In such "small-world" PPI networks most pairs of nodes can be linked to each other by relatively short chains of interactions involving just a few intermediate proteins [1]. While globally connected architecture facilitates biological signaling and possibly ensures a robust functioning of the cell following a random failure of its components [2], it also presents a potential problem by providing a conduit for propagation of undesirable cross-talk between individual functional modules and pathways. Indeed, large (several-fold) changes in proteins' levels in the course of activation or repression of a certain functional module affect bound concentrations of their immediate interaction partners. These changes have a potential to cascade down a small-world PPI network affecting the equilibrium between bound and unbound concentrations of progressively more distant neighbors including those in other functional modules. Most often such indiscriminate propagation would represent an undesirable effect which has to be either tolerated or corrected by the cell. On the other hand, a controlled transduction of reversible concentration changes along specific conduits may be used for biologically meaningful signaling and regulation. A routine and well known example of such regulation is inactivation of a protein by sequestration with its strong binding partner.

In this study we quantitatively investigate how large concentration changes propagate in the PPI network of yeast *S. cerevisiae*. We

focus on the non-catalytic or reversible binding interactions whose equilibrium is governed by the Law of Mass Action (LMA) and do not consider irreversible, catalytic processes such as protein phosphorylation and dephosphorylation, proteolytic cleavage, etc. While such catalytic interactions constitute the most common and best studied mechanism of intracellular signaling, they represent only a rather small minority of all protein-protein physical interactions (for example, only ~5% links in the yeast network used in our study involve a kinase).

Furthermore, the balance between free and bound concentrations of proteins matters even for irreversible (catalytic) interactions. For example, the rate of a phosphorylation reaction depends on the availability of free kinases and substrate proteins which are both controlled by the LMA equilibrium calculated here. Thus perturbations of equilibrium concentrations considered in this study could be spread even further by other mechanisms such as transcriptional and translational regulation, and irreversible posttranslational protein modifications.

Results

To illustrate general principles on a concrete example, in this study we used a highly curated genome-wide network of protein-protein physical interactions in yeast (*S. cerevisiae*), which, according to the BIOGRID database [3], were independently confirmed in at least two publications. We combined this network with a genome-wide dataset of protein abundances in the log-phase growth in rich medium, measured by the TAP-tagged western blot technique [4]. Average protein concentrations in this dataset range between 50 and 1,000,000 molecules/cell with the median value around 3000 molecules/cell. After keeping only the interactions between proteins with known concentrations we were left with 4185 binding interactions among 1740 proteins (Table S1). The BIOGRID database [3] lists all interactions as pairwise and thus lacks information about multi-protein complexes larger than dimers. Thus in the main part of this study we consider only homo- and hetero-dimers and ignore the formation of higher-order complexes. In the Supplementary materials we show that the reliable data on multi-protein complexes can be easily incorporated into our analysis. Furthermore, we demonstrate that taking into account such complexes leaves our results virtually unchanged (see supplementary Table S4 and Fig. S3).

Conflict of interest footnote placeholder

This paper was submitted directly to the PNAS office.

† Corresponding author, email: maslov@bnl.gov

‡ Corresponding author, email: slava@ariadnegenomics.com

©2007 by The National Academy of Sciences of the USA

The state of the art genome-wide PPI datasets lack information on dissociation constants K_{ij} of individual interactions. The only implicit assumption is that the binding is sufficiently strong to be detectable by a particular experimental technique (some tentative bounds on dissociation constants detectable by different techniques were reported recently [5]). A rough estimate of the average binding strength in functional protein-protein interactions could be obtained from the PINT database [6]. This database contains about 400 experimentally measured dissociation constants between wildtype proteins from a variety of organisms. In agreement with predictions of Refs. [7, 8] the histogram of these dissociation constants has an approximately log-normal shape. The average relevant for our calculations is that of the *association* constant $\langle 1/K_{ij} \rangle = 1/(5nM)$. Common sense dictates that the dissociation constant of a functional binding between a pair of proteins should increase with their abundances. The majority of specific physical interactions between proteins are neither too weak (to ensure a considerable number of bound complexes) nor unnecessarily strong. Indeed, there is little evolutionary sense in increasing the binding strength between a pair of proteins beyond the point when both proteins (or at least the rate limiting one) spend most of their time in the bound state. The balance between these two opposing requirements is achieved by the value of dissociation constant K_{ij} equal to a fixed fraction of the largest of the two abundances C_i and C_j of interacting proteins. In our simulations we used $K_{ij} = \max(C_i, C_j)/20$ in which case the average association constant nicely agrees with its empirical value ($1/(5nM)$) observed in the PINT database [6]. In addition to this, perhaps, more realistic assignment of dissociation constants we also simulated binding networks in which dissociation constants of all 4185 edges in our network are *equal to each other* and given by $1nM$, $10nM$, $100nM$, and $1\mu M$.

Numerical calculation of bound and free (unbound) equilibrium concentrations. The Law of Mass Action (LMA) relates the free (unbound) concentration F_i of a protein to its total (bound and unbound) concentration C_i as

$$F_i = \frac{C_i}{1 + \sum_j F_j / K_{ij}} \quad . \quad [1]$$

Here the sum is over all specific binding partners of the protein i with free concentrations F_j and dissociation constants K_{ij} . While in the general case these nonlinear equations do not allow for an analytical solution for F_i , they are readily solved numerically e.g. by successive iterations.

Concentration-coupled proteins. To investigate how large changes in abundances of individual protein affect the equilibrium throughout the PPI network we performed a systematic numerical study in which we recalculated the equilibrium free concentrations of all protein nodes following a twofold increase in the total concentration of just one of them: $C_i \rightarrow 2C_i$. This was repeated for the source of twofold perturbation spanning the set of all 1740 of proteins in our network [9]. The magnitude of the initial perturbation was selected to be representative of a typical shift in gene expression levels or protein abundances following a change in external or internal conditions. Thus here we simulate the propagation of functionally relevant changes in protein concentrations and not that of background stochastic fluctuations. A change in the free concentration F_j of another protein was deemed to be significant if it exceeded the 20% level, which according to Ref. [10] is the average magnitude of cell-to-cell variability of protein abundances in yeast. We refer to such protein pairs $i \rightarrow j$ as *concentration-coupled*. The detection threshold could be raised simultaneously with the magnitude of the initial perturbation. For example, we found that the list of concentration-coupled pairs changes very little if instead of twofold (+100%) perturbation

and the 20% detection threshold one applies a sixfold (+500%) initial perturbation and twofold (100%) detection threshold.

In general we found that lists of concentration-coupled proteins calculated for different assignments of dissociation constants strongly overlap with each other. For example, more than 80% of concentration-coupled pairs observed for the variable $K_{ij} = \max(C_i, C_j)/20$ assignment described above were also detected for the uniform assignment $K_{ij} = \text{const} = 10nM$ (for more details see the supplementary table S3) This relative robustness of our results allowed us to use the latter conceptually simplest case to illustrate our findings in the rest of the manuscript.

The complete list of concentration-coupled pairs is included in the supplementary materials. Given the incompleteness and uncertainty in our knowledge of the network topology, protein abundances, and values of dissociation constants, these lists provide only a rough estimate of the actual magnitude of perturbations that could be measured experimentally.

Central observations. We found that:

- *On average*, the magnitude of cascading changes in equilibrium free concentrations exponentially decays with the distance from the source of a perturbation. This explains why, despite a globally connected topology, individual modules in such networks are able to function fairly independently.
- Nevertheless, specific favorable conditions identified in our study cause perturbations to selectively affect proteins at considerable network distances (sometimes as far as four steps away from the source). This indicates that in general, such cascading changes *could not be neglected* when evaluating the consequences of systematic changes in protein levels, e.g. in response to environmental factors, or in gene knockout experiments. Conditions favorable for propagation of perturbations combine high yet monotonically decreasing concentrations of all heterodimers along the path with low free (unbound) concentrations of intermediate proteins. While reversible protein binding links are symmetric, the propagation of concentration changes is usually asymmetric with the preferential direction pointing down the gradient in the total concentrations of proteins.

Examples of multi-step cascading changes. In Fig. 1AB we illustrate these observations using two examples. In each of these cases the twofold increase in the abundance of just one protein (marked with the yellow circle in the center of each panel) has significantly ($> 20\%$) affected equilibrium free concentrations of a whole cluster of proteins some as far as 4 steps away from the source of the perturbation. However, the propagation beyond immediate neighbors is rather specific. For example, in the case of SUP35 (Fig. 1A) only 1 out of 169 of its third nearest neighbors were affected above the 20% level. Note that changes in free concentrations generally sign-alternate with the network distance from the source. Indeed, free concentrations of immediate binding partners of the perturbed protein usually drop as more of them become bound in heterodimers with it. This, in turn, lowers concentrations of the next-nearest heterodimers and thus *increases* free concentrations of proteins at distance 2 from the source of perturbation, and so on.

Exponential decay with the network distance. The results of our quantitative network-wide analysis of these effects are summarized in Fig. 2 and Table 1. From Fig. 2 one concludes that the fraction of proteins with significantly affected free concentrations rapidly (exponentially) decays with the length L of the shortest path (network

distance) from the perturbed protein. The same statement holds true for bound concentrations if the distance is measured as the shortest path from the perturbed protein to any of the two proteins forming a heterodimer. Thus, on average, the propagation of concentration changes along the PPI network is indeed considerably damped. On the other hand, from Table 1 one concludes that the total number of multi-step chains along which concentration changes propagate with little attenuation remains significant for all but the largest values of the dissociation constant. These two observations do not contradict each other since the number of proteins separated by distance L (the last column in Table 1) rapidly grows with L .

Conditions favoring the multi-step propagation of perturbations. What conditions favor the multi-step propagation of perturbations along particular channels? In Fig. 3A we show a group of highly abundant proteins along with all binding interactions between them. Then on panel B of the same figure we show only those interactions that according to our LMA calculation give rise to highly abundant heterodimers (equilibrium concentration >1000 per cell). This breaks the densely interconnected subnetwork drawn in the panel A into 10 mutually isolated clusters. Some of these clusters contain pronounced linear chains which serve as conduits for propagation of concentration perturbations. The fact that perturbations indeed tend to propagate via highly abundant heterodimers is illustrated in the next panel (Fig. 3C) where red arrows correspond to concentration-coupled nearest neighbors $A \rightarrow B$. Evidently, the edges in panels B and C largely (but not completely) coincide. Additionally, the panel C defines the preferred direction of propagation of perturbations from a more abundant protein to its less abundant binding partners.

To further investigate what causes concentration changes to propagate along particular channels we took a closer look at eight three-step chains $A \rightarrow A_1 \rightarrow A_2 \rightarrow B$ with the largest magnitude of perturbation of the last protein B (twofold detection threshold following a twofold initial perturbation). The identification of intermediate proteins A_1 and A_2 was made by a simple optimization algorithm searching for the largest overall magnitude of intermediate perturbations along all possible paths connecting A and B .

Inspection of the parameters of these chains shown in Fig. 4 allows one to conjecture that for a successful transduction of concentration changes, the following conditions should be satisfied:

- Heterodimers along the whole path have to be of sufficiently high concentration D_{ij} .
- Intermediate proteins have to be highly sequestered. That is to say, in order to reduce buffering effects free-to-total concentration ratios F_i/C_i should be sufficiently low for all but the last protein in the chain.
- Total concentrations C_i should gradually decrease in the direction of propagation. Thus propagation of perturbations along virtually all of these long conduits is unidirectional and follows the gradient of concentration changes (a related concept of a “gradient network” was proposed for technological networks in Ref. [11]).
- Free concentrations F_i should alternate between relatively high and relatively low values in such a way that free concentrations of proteins at steps 2 and 4 have enough “room” to go down. The two apparent exceptions to this rule visible in Fig. 4 may be optimized to respond to a drop (instead of increase) in the level of the first protein.

These findings are in agreement with our more detailed numerical and analytical analysis of propagation of fluctuations presented in [12] and illustrated for simple networks in the Supplementary materials. In [12] we demonstrated that the linear response of the LMA equilibrium to *small* changes in protein abundances could be approximately mapped to a current flow in the resistor network in which heterodimer concentrations play the role of conductivities (which need to be large for a good transmission) while high F_i/C_i ratios result in the net loss of the perturbation “current” on such nodes and thus need to be minimized.

Discussion

Robustness with respect to assignment of dissociation constants. It has been often conjectured that the qualitative dynamical properties of biological networks are to a large extent determined by their topology rather than by quantitative parameters of individual interactions such as their kinetic or equilibrium constants (for a classic success story see e.g. [13]). Our results generally support this conjecture, yet go one step further: we observe that the response of reversible protein-protein binding networks to large changes in concentrations strongly depends not only on topology but also on abundances of participating proteins. Indeed, perturbations tend to preferentially propagate via paths in the network in which abundances of intermediate proteins monotonically decrease along the path (see Fig. 3). Thus by varying protein abundances while strictly preserving the topology of the underlying network, one can select different conduits for propagation of perturbations.

On the other hand our results indicate that these conduits are to a certain degree insensitive to the choice of dissociation constants. In particular, we found (see Fig. 5) that equilibrium concentrations of dimers and the remaining free (unbound) concentrations of individual proteins calculated for two different K_{ij} assignments ($K_{ij} = \text{const} = 5\text{nM}$ and $K_{ij} = \max(C_i, C_j)/20$ with the inverse mean of 5nM) had a high Spearman rank correlation coefficient of 0.89 and even higher linear Pearson correlation coefficient of 0.98. The agreement was especially impressive in the upper part of the range of dimer concentrations (see Fig. 5). For example, the typical difference between dimer concentrations above 1000 molecules/cell was measured to be as low as 40%. As we demonstrated above it is exactly these highly abundant heterodimers that form the backbone for propagation of concentration perturbations. Thus it should come as no surprise that sets of concentration-coupled protein pairs observed for different K_{ij} assignments also have a large ($\sim 70\text{-}80\%$) overlap with each other (see the supplementary table S3).

Such degree of robustness with respect quantitative parameters of interactions can be partially explained by the following observation: proteins whose abundance is higher than the sum of abundances of all of their binding partners cannot be fully sequestered into heterodimers for any assignment of dissociation constants. As we argued above, such proteins with substantial unbound concentrations considerably dampen the propagation of perturbations, and thus cannot participate in highly conductive chains. Another argument in favor of this apparent robustness is based on extreme heterogeneity of wildtype protein abundances (in the dataset of Ref. [4] they span 5 orders of magnitude). In this case concentrations of heterodimers depend more on relative abundances of two constituent proteins than on the corresponding dissociation constant (within a certain range).

In a separate numerical control experiment we verified that the main results of this study are not particularly sensitive to false positives and false negatives in the network topology inevitably present even in the best curated large-scale data. The percentage of

concentration-coupled pairs surviving a random removal or addition of 20% of links in the network generally ranges between 60% and 80% (see supplementary table S2).

Genetic interactions. The effects of concentration perturbations discussed above could explain some of the genetic interactions between proteins. Consider for example a “dosage rescue” of a protein *A* by a protein *B*, or the correction of an abnormal phenotype caused by deletion or other type of inactivation of *A* by overexpression of *B*. One possible mechanism behind this effect is that the knockout of *A* and overexpression of *B* affect the LMA equilibrium in opposite directions and to some extent cancel one another. In order for this mechanism to be applicable (albeit tentatively), concentrations of both *A* and *B* must be simultaneously coupled (in the sense used throughout this work) to at least one crucial protein *C* whose free or bound concentration has to be maintained at or close to wildtype levels. To assess this hypothesis, we analyzed the set of 772 dosage rescue pairs involving proteins from the PPI network used in this study of 2531 dosage rescue pairs listed in the BIOGRID database [3]. For 136 pairs (or 18% of all dosage rescue pairs), we were able to identify one or more putative “rescued” protein whose free concentration was considerably (by >20%) affected by changes in abundances of both *A* and *B* (see supplementary Table S5). This overlap is highly statistically significant, having the Fisher’s exact test p-value around 10^{-216} . Even more convincing evidence that perturbations to the LMA equilibrium state cause some of genetic interactions is presented in Figure 6. It plots the fraction of protein pairs at distance *L* from each other in the PPI network that are known to dosage rescue each other. From this figure one concludes that proteins separated by distances 1,2, and 3 are significantly more likely to genetically interact with each other than one expects by pure chance alone (the expected background level is marked with a dashed line or better yet visible as a plateau for large values of *L*). Furthermore, the slope of the exponential decay in the fraction of dosage rescue pairs as a function of *L* is roughly consistent with that shown in Fig. 2 for the fraction of concentration-coupled pairs.

Possibility of functional signaling and regulation mediated by multi-step reversible protein interactions. Another intriguing possibility raised by our findings is that multi-step chains of reversible protein-protein bindings might in principle be involved in meaningful intracellular signaling and regulation. There are many well-documented cases in which one-step “chains” are used to reversibly deactivate individual proteins by the virtue of sequestration with their binding partner(s). An example involving a longer regulatory chain of this type is the control of activity of condition-specific sigma factors in bacteria. In its biologically active state, a given sigma factor is bound to the RNA polymerase complex. Under normal conditions it is commonly kept in an inactive form by the virtue of a strong binding with its specific anti-sigma factor (anti-sigma factors are reviewed in [14]). In several known cases the concentration of the anti-sigma factor in turn is controlled by its binding with the specific anti-anti sigma factor [14]. The existence of such experimentally confirmed three-step regulatory chains in bacteria hints at the possibility that at least some of the longer conduits we detected in yeast could be used in a similar way.

Application to microarray data analysis. In order to unequivocally detect cascading perturbations, in our simulations we always modified the total concentration of just one protein at at time. In more realistic situations, expression levels of a whole cluster of genes change, for example, in response to a shift in environmental conditions. Our general methods could be easily extended to incorporate

this scenario. With the caveat that changes in expression levels of genes reflect changes in overall abundances of corresponding proteins, our algorithm allows one to calculate the impact of an external or internal stimulus measured in a microarray on free and bound concentrations of all proteins in the cell. Including such indirectly perturbed targets could considerably extend the list of proteins affected by a given shift in environmental conditions. Simultaneous shifts in expression levels of several genes may amplify changes of free concentrations of some proteins and/or mutually inhibit changes of others.

Effects of intracellular noise. Another implication of our findings is for intracellular noise, or small random changes in total concentrations C_i of a large number of proteins. The randomness, smaller magnitude, and the sheer number of the involved proteins characterize the differences between such noise and systematic several-fold changes in the total concentration of one or several proteins considered above. Our methods allow one to decompose the experimentally measured [10] noise in total abundances of proteins into biologically meaningful components (free concentrations and bound concentrations within individual protein complexes). Given a fairly small magnitude of fluctuations in protein abundances (on average around 20% [10]), one could safely employ a computationally-efficient linear response algorithm (see [12]). Several recent studies [15], [16], [10] distinguish between the so-called extrinsic and intrinsic noise. The extrinsic noise corresponds to synchronous or correlated shifts in abundance of multiple proteins which, among other things, could be attributed to variation in cell sizes and their overall mRNA and protein production or degradation rates. Conversely, the intrinsic noise is due to stochastic fluctuations in production and degradation and thus lacks correlation between different proteins. We found that extrinsic and intrinsic noise affect equilibrium concentrations of proteins in profoundly different ways. In particular, while multiple sources of the extrinsic noise partially (yet not completely) cancel each other, intrinsic noise contributions from several sources can sometimes add up and cause considerable fluctuations in equilibrium free and bound concentrations of particular proteins (see Figure 7).

Limitations of the current approach and directions for further studies. In our study we used a number of fundamental approximations and idealizations including the assumption of spatially uniform concentrations of proteins, the neglect of temporal dynamics or, equivalently, the assumption that all concentrations have sufficient time to reach their equilibrium values, the continuum approximation neglecting the discrete nature of proteins and their bound complexes, etc. Another set of approximations was mostly due to the lack of reliable large-scale data quantifying these effects. They include not taking into account the effects of cooperative binding within multi-protein complexes, using a relatively small number (81) of well curated multi-protein complexes used in our study (see supplementary materials), neglecting systematic changes in protein abundances in the course of the cell cycle, etc. We do not expect these effects to significantly alter our main qualitative conclusions, namely, the exponential decay of the amplitude of changes in equilibrium concentrations, the existence of 3-4 step chains that nevertheless successfully propagate concentration changes, and the general conditions that enhance or inhibit such propagation.

In the future we plan to extend our study of fluctuations in equilibrium concentrations by incorporating the effects of protein diffusion (non-uniform spatial concentration) and kinetic effects. Another interesting avenue for further research is to apply the concept of “potential energy landscape” (for definitions see [17] and references therein) to reversible processes governed by the law of mass action,

such as e.g. the equilibrium in protein binding networks. In the past this concept was applied to processes involving catalytic, irreversible protein-protein interactions such as e.g. phosphorylation by kinases or regulation by transcription factors. In this case it helped to reveal the robustness of regulatory networks in the cell cycle [18] and in a simple two-protein toggle switch [19].

Methods

Source of interaction and concentration data The curated PPI network data used in our study is based on the 2.020 release of the BIOGRID database [3]. We kept only pairs of physically interacting proteins that were reported in at least two publications using the following experimental techniques: Affinity Capture-MS (28172 pairs), Affinity Capture-RNA (55 pairs), Affinity Capture-Western (5710 pairs), Co-crystal Structure (107 pairs), FRET (43 pairs), Far Western (41 pair), Two-hybrid (11935 pairs). That left us with 5798 non-redundant interacting pairs. Further restriction for both proteins to have experimentally measured total abundance [4] narrowed it down to 4185 distinct interactions among 1740 yeast proteins.

The list of manually curated yeast protein complexes was obtained from the latest release (May 2006) of the MIPS CYGD database [20, 21]. The database contains 1205 putative protein complexes 326 of which are not coming from systemic analysis studies (high-throughput MS experiments). In the spirit of using only the confirmed PPI data we limited our study to these manually curated 326 complexes. For 99 of these complexes the MIPS database lists 3 or more constituent proteins. After elimination of proteins with unknown total concentrations we were left with 81 multi-protein complexes.

1. Wagner, A. (2001) *Molecular Biology and Evolution* **18**, 1283–1292.
2. Jeong, H., Mason, SP. Barabasi, AL, & Oltvai, ZN (2001) *Nature* **411**(6833), 41–42.
3. Stark, Chris, Breitkreutz, Bobby-Joe, Reguly, Teresa, Boucher, Lorrie, Breitkreutz, Ashton, & Tyers, Mike (2006) *Nucl. Acids Res.* **34**(suppl_1), D535–539.
4. Ghaemmaghami, S., Huh, W.K., Bower, K., Howson, R.W., Belle, A., Dephoure, N., & O'Shea, E.K. (2003) *Nature* **425**, 737–741.
5. Piehler, J. (2005) *Curr Opin in Struct Biol* **15**, 4–14.
6. Kumar, MD & Gromiha, MM (2006) *Nucleic Acids Res.* **34**, D195–D198.
7. Lancet, D., Sadovsky, E., & Seidemann, E. (1993) *Proceedings of the National Academy of Sciences* **90**(8), 3715–3719.
8. Deeds, E.J., Ashenberg, O., & Shakhnovich, E.I. (2006) *Proceedings of the National Academy of Sciences* **103**(2), 311–316.
9. As an alternative to this computationally expensive approach we also tried the linear response matrix formalism [12] relating small changes in F_j to the ones in C_i . We found the linear response algorithm to be much less computationally expensive, while still providing remarkably good approximation to directly computed results even for large changes in protein levels.
10. Newman, J.R.S., Ghaemmaghami, S., Ihmels, J., Breslow, D.K., Noble, M., DeRisi, J.L., & Weissman, J.S. (2006) *Nature* **441**, 840–846.
11. Toroczkai, Z. & Bassler, K.E. (2004) *Nature* **428**(716), 170.
12. Maslov, S., Sneppen, K., & Ispolatov, I. (2007) *New Journal of Physics* in press. Preprint at <http://arxiv.org/abs/q-bio.MN/0611026>.
13. vonDassow, G., Meir, E., Munro, EM, & Odell, GM (2000) *Nature* **406**(6792), 188–192.
14. Hughes, K.T. & Mathee, K. (1998) *Annual Review of Microbiology* **52**(1), 231–286.
15. Elowitz, M.B., Levine, A.J., Siggia, E.D., & Swain, P.S. (2002) *Science* **297**(5584), 1183.
16. Raser, J.M. & O'Shea, E.K. (2005) *Science* **309**(5743), 2010–2013.
17. Ao, P. (2004) *Journal of Physics A: Mathematical and General* **37**(3), L25–L30.
18. Wang, J., Huang, B., Xia, X., & Sun, Z. (2006) *PLoS Computational Biology* **2**(11), e147, 1385.
19. Kim, K. & Wang, J. (2007) *PLoS Computational Biology* **3**(e60), 0656.
20. Guldener, U., Munsterkotter, M., Kastenmuller, G., Strack, N., vanHelden, J., Lemmer, C., Richelles, J., Wodak, SJ, Garcia-Martinez, J., Perez-Ortin, JE, & others, (2005) *Nucleic Acids Res* **33**, 364–368.
21. Mewes, HW, Heumann, K., Kaps, A., Mayer, K., Pfeiffer, F., Stocker, S., & Frishman, D. (1999) *Nucleic Acids Research* **27**(1), 44–48.

Genetic interactions of dosage rescue type were also obtained from the BIOGRID database. There are 772 pairs of dosage rescue interactions among 1740 proteins participating in our PPI network (the full list contains 2531 dosage rescue pairs).

Numerical algorithms. The numerical algorithm calculating all free concentrations F_i given the set of total concentrations C_i and the matrix of dissociation constants K_{ij} was implemented in MATLAB 7.1 and is available for downloading on <http://www.cmth.bnl.gov/~maslov/programs.htm>. It consists of iterating the Eq. 1 starting with $F_i = C_i$. Iterations stop once relative change of free concentration on every node in the course of one iteration step becomes smaller than 10^{-8} which for networks used in our study takes less than a minute on a desktop computer. When necessary, multiprotein complexes are incorporated into this algorithm as described in the Supplementary Materials.

The effects of large concentration perturbations was calculated by recalculating free concentrations following a twofold increase in abundance of a given perturbed protein. The effects of small perturbations such as those of concentration fluctuations were calculated using the faster linear response matrix formalism described elsewhere [12].

We thank Kim Sneppen for valuable discussions and contributions in early phases of this project. This work was supported by National Institute of General Medical Sciences Grant 1 R01 GM068954-01. Work at Brookhaven National Laboratory was carried out under Division of Material Science, U.S. Department of Energy Contract DE-AC02- 98CH10886. S.M.s visit to the Kavli Institute for Theoretical Physics, where part of this work was accomplished, was supported by National Science Foundation Grant PHY05-51164.

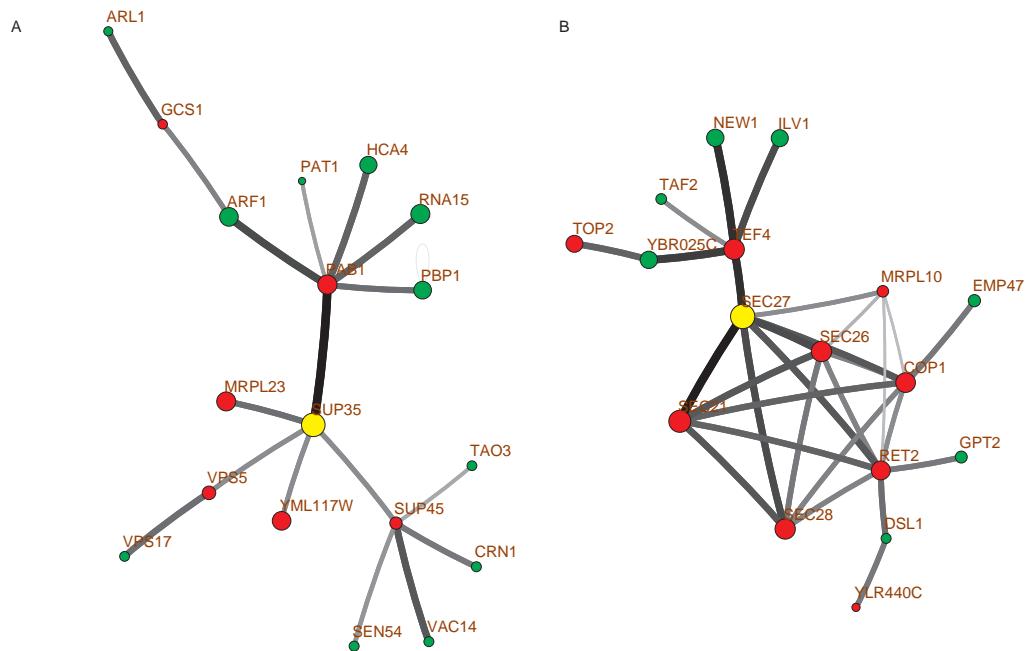


Fig. 1. Two cases of propagation of large concentration changes in the yeast protein binding network. The total (bound + unbound) concentration of the protein marked with the yellow circle (the SUP35 protein (A), the SEC27 protein (B)) was increased twofold from its wildtype value in the rich growth medium [4]. Red and green circles mark all other proteins whose equilibrium free (unbound) concentrations have increased (green) or decreased (red) by more than 20%. The area of each circle is proportional to the logarithm of the change in free concentration. Edges show all physical interactions among this group of proteins with the shade of gray proportional to the logarithm of the equilibrium concentration of the corresponding dimer calculated for $K_{ij} = \text{const} = 10\text{nM}$.

Table 1. The number of concentration-coupled pairs of yeast proteins separated by network distance L . Numerical simulations (twofold initial perturbation, 20% detection threshold) were performed for different assignment of dissociation constants: $K_{ij} = \max(C_i, C_j)/20$ (column 2), $K_{ij} = \text{const} = 1\text{nM}, 10\text{nM}, 0.1\mu\text{M}, 1\mu\text{M}$ (columns 3–6). The column 7 lists the total number of protein pairs at distance L .

L	var. 5nM	1nM	10nM	0.1 μM	1 μM	all
1	2003	2469	1915	1184	387	8168
2	415	1195	653	206	71	29880
3	15	159	49	8	0	87772
4	2	60	19	0	0	228026
5	0	3	0	0	0	396608

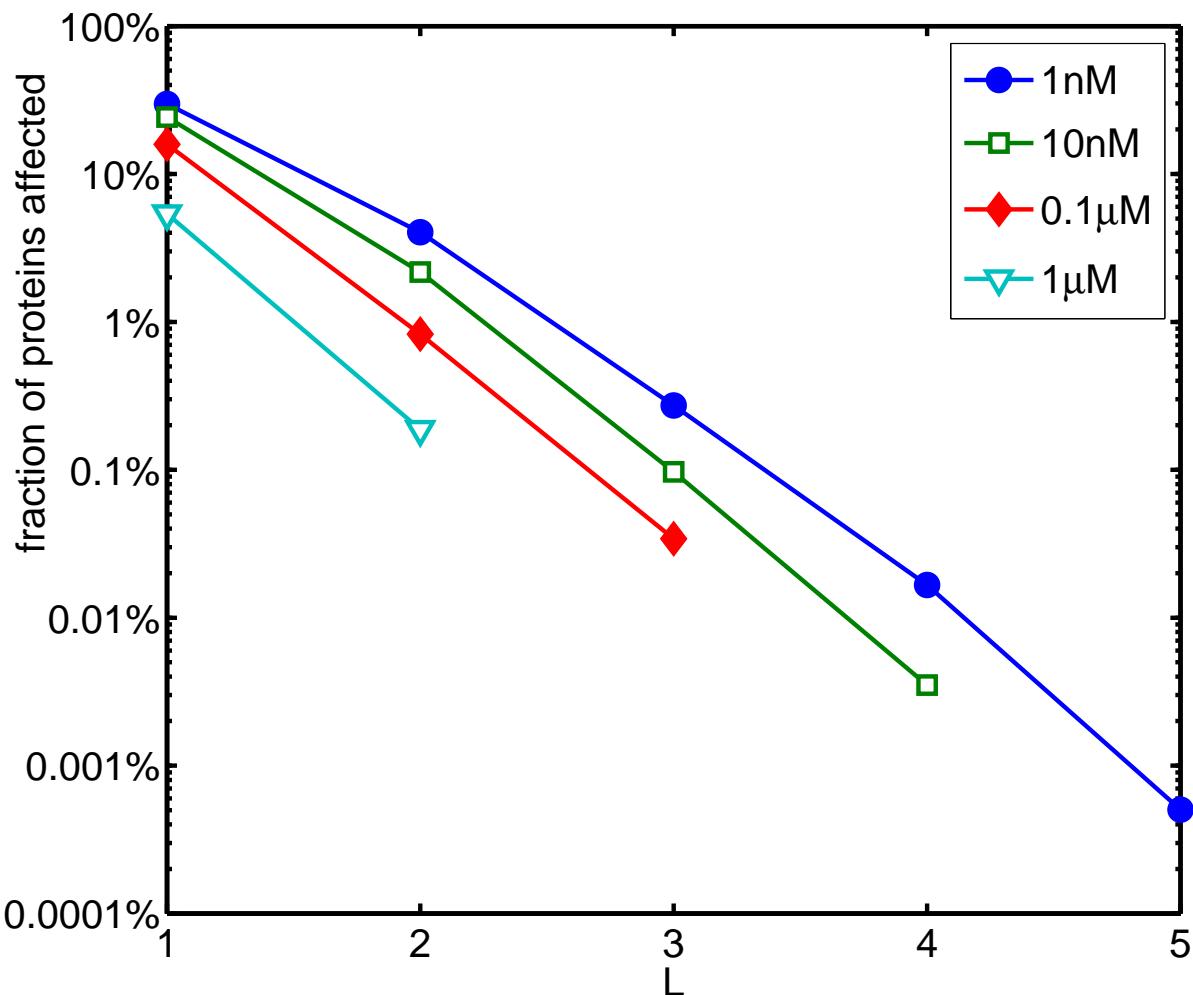


Fig. 2. Indiscriminate propagation of concentration perturbations is exponentially suppressed. The fraction of proteins with free concentrations affected by more than 20% among all proteins at network distance L from the perturbed protein. Different curves correspond to simulations with $K_{ij} = \text{const} = 1\text{nM}$ (solid circles), 10nM (empty squares), $0.1\mu\text{M}$ (solid diamonds), and $1\mu\text{M}$ (empty triangles).

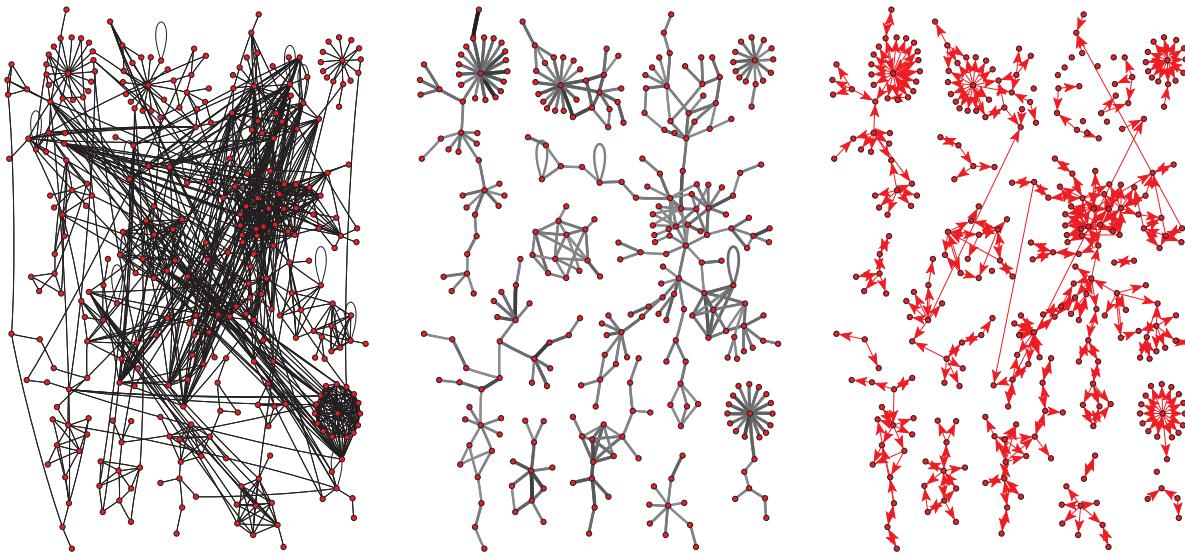


Fig. 3. A) All binding links between a subset of 312 highly abundant proteins. B) Binding links characterized by high concentration of heterodimers (> 1000 molecules/cell). The level of gray of binding links scales with the logarithm of concentration of the corresponding heterodimer. C) Concentration-coupled proteins $A \rightarrow B$ with the property that a twofold increase in the abundance A reduces free concentration of its immediate binding partner B by 20% or more. Note that links roughly coincide with highly abundant dimers shown in the panel B. Arrows reveal the preferential direction of propagation of perturbations.

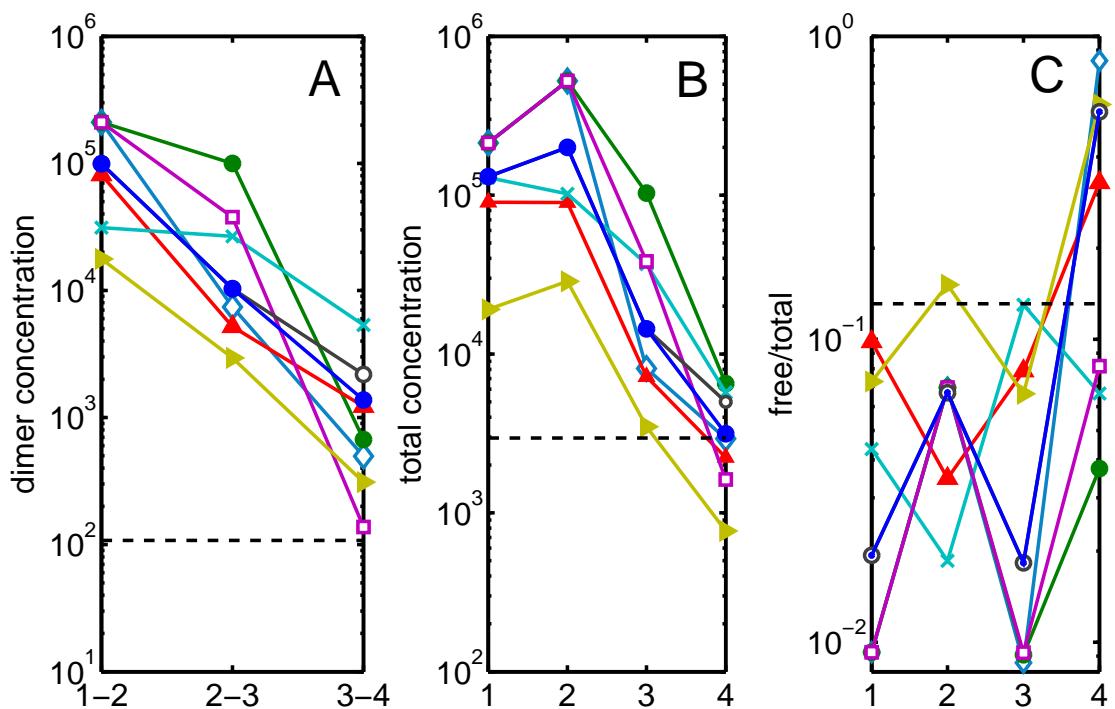


Fig. 4. Parameters of the eight three-step chains that exhibit the best transduction of concentration changes: Heterodimer concentrations D_{ij} (A) for three binding links along the chain. Total concentrations C_i (B) and free-to-total concentration ratios F_i/C_i (C) of the four proteins involved in these chains. Dashed lines correspond to network-wide geometric averages of the corresponding quantities: $\langle D_{ij} \rangle \sim 100$ copies/cell, $\langle C_i \rangle \sim 3000$ copies/cell, and $\langle F_i/C_i \rangle = 13\%$.

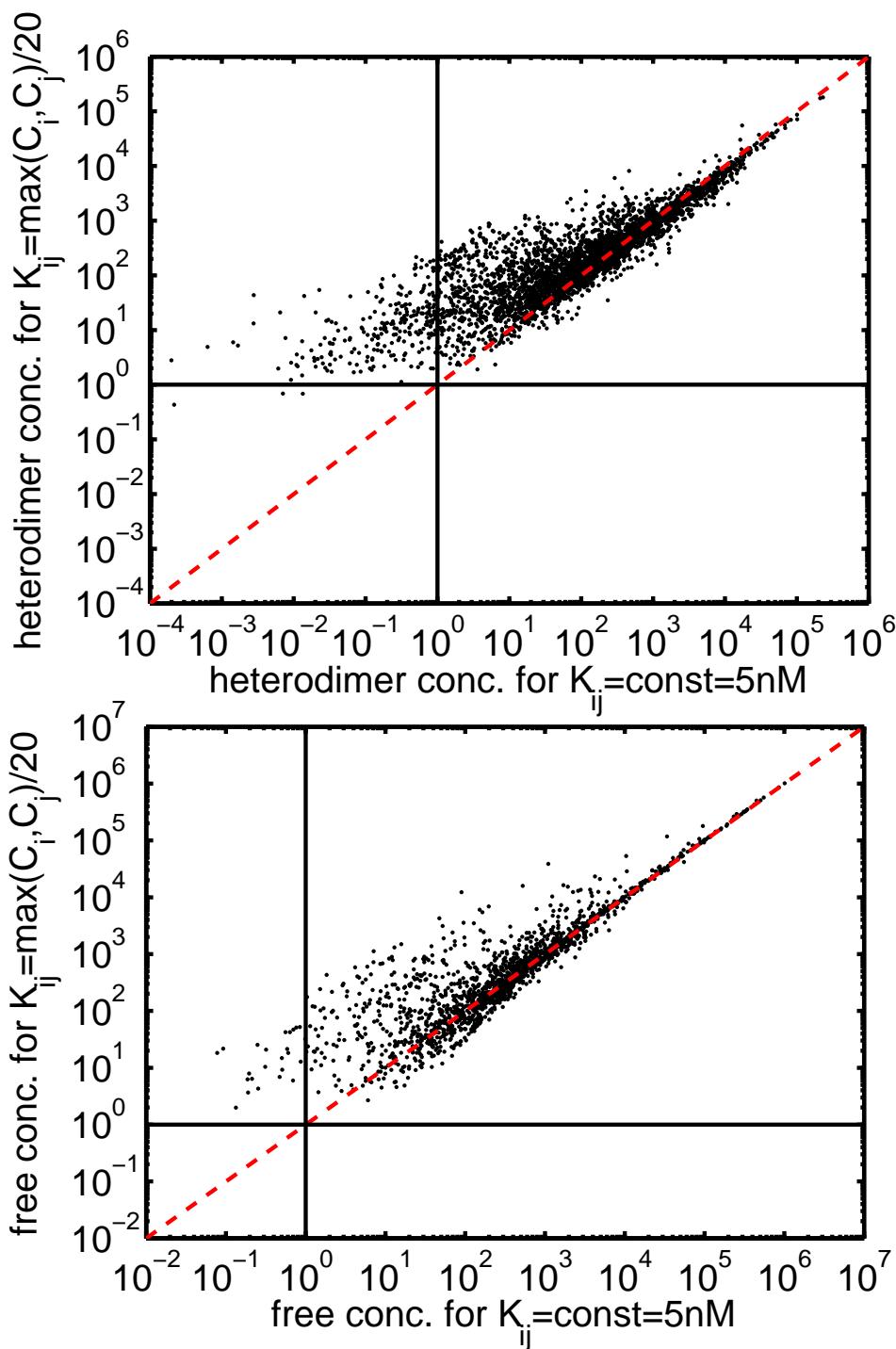


Fig. 5. The scatter plot of 4185 bound concentrations D_{ij} (panel A) and 1740 free concentrations F_i (panel B) calculated for two different assignments of dissociation constants to links in the PPI network. The x-axis was computed for the homogeneous assignment $K_{ij} = \text{const} = 5\text{nM}$, while the y-axis was computed for the heterogeneous assignment $K_{ij} = \max(C_i, C_j)/20$ with the same average strength. The dashed lines along the diagonals are drawn at $x = y$, while the horizontal and vertical solid lines denote the concentration of 1 molecule/cell. Note that equilibrium concentrations in the upper part of their range (e.g. above 1000 molecules/cell) are nearly independent of the choice of K_{ij} . Also, our choice of heterogeneous assignment nearly eliminates free or bound concentrations in a biologically unreasonable range <1 molecules/cell

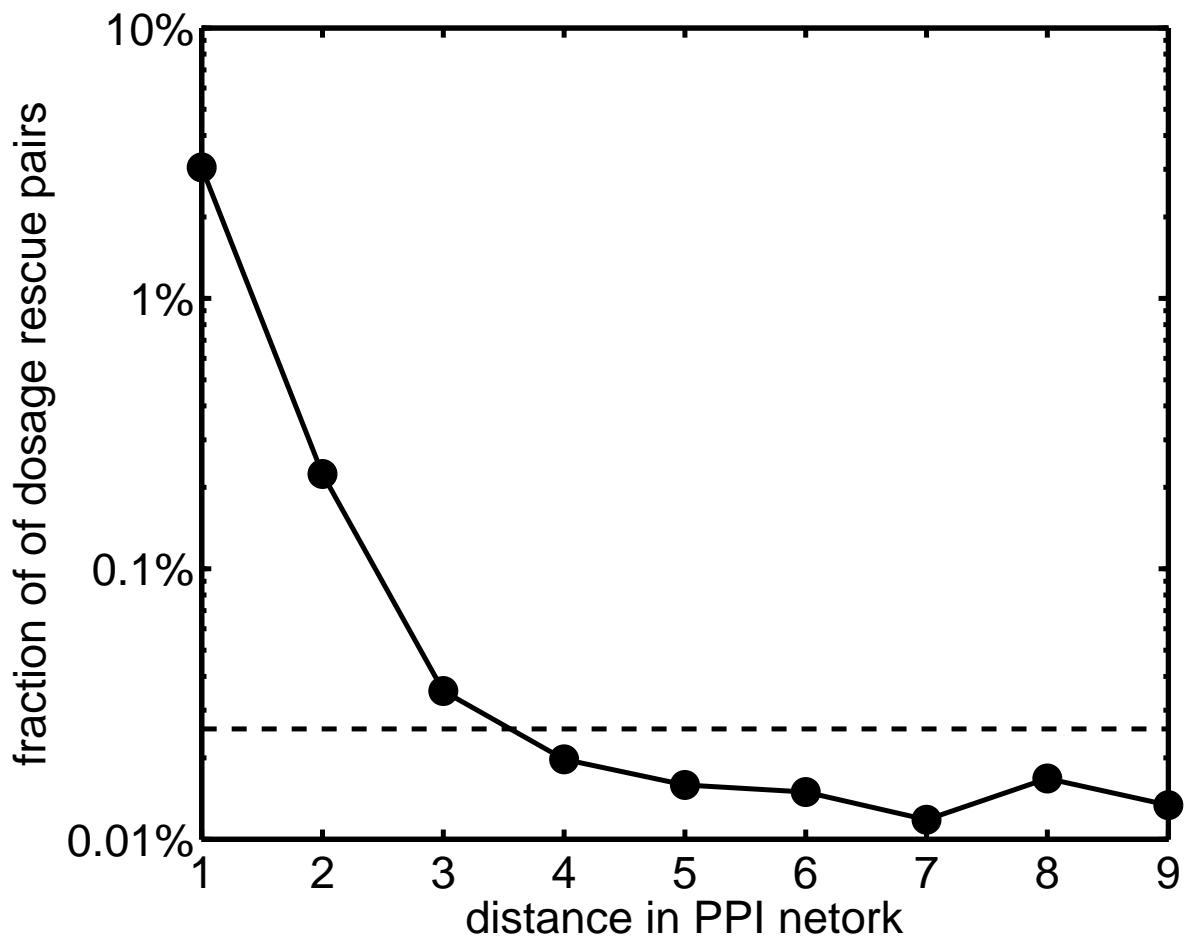


Fig. 6. The fraction of dosage rescue protein pairs separated by distance L in the PPI network. Note that pairs at distances 1,2 and 3 are significantly overrepresented over the background level marked with dashed line ($772/1740^2$) or visible as a plateau at large distances L . The exponential decay constant at low values of L is consistent with that in Fig. 2.

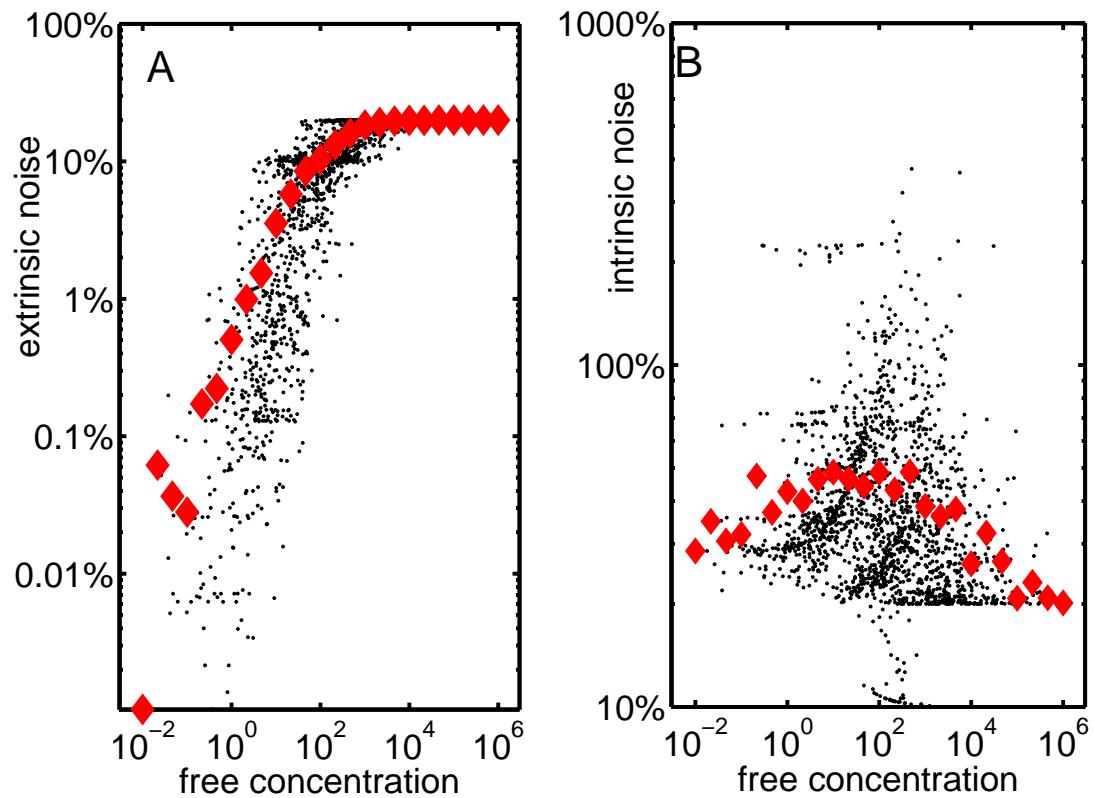


Fig. 7. The magnitude of extrinsic (panel A) and intrinsic noise in free concentrations F_i of proteins when their total concentrations C_i fluctuate by 20%. In this plot we used $K_{ij} = \text{const} = 1\text{nM}$. One can see that while the extrinsic noise is suppressed in the low concentrations region, the intrinsic one is uniformly high and reaches as much as >300% in the mid- F_i range.